

# Nanomechanical Friction: a source of nonlinear damping in CNT resonators

## - Nanomechanical manipulation experiments and modeling -

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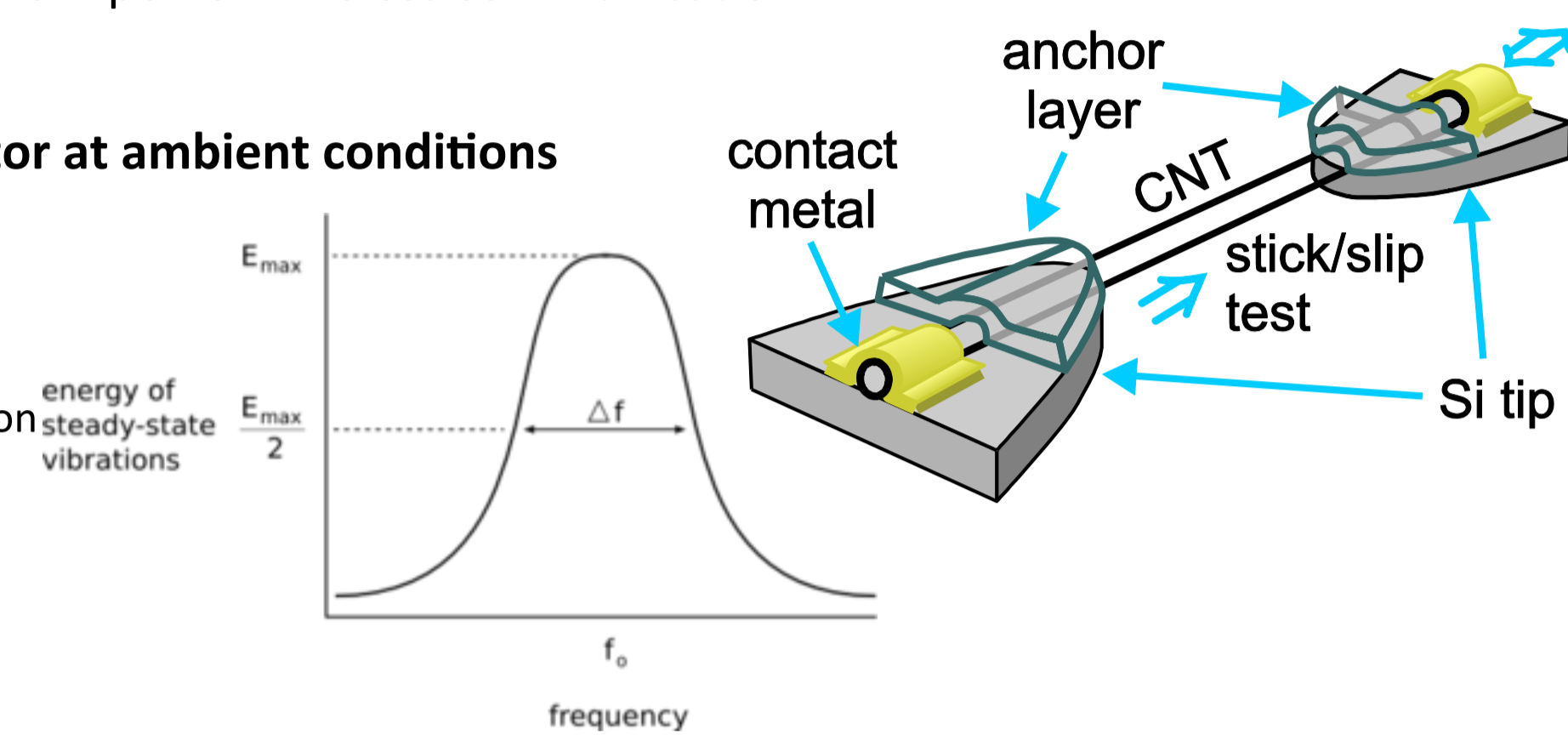
### Motivation

Mechanical properties of single walled carbon nanotubes (SWCNTs) and nanowires are critical for various nanoelectromechanical systems such as Giga Hertz resonators for ultra-low mass and chemical sensing, high sensitivity pressure sensing and low-power wireless communication

**Major limiting so far: poor Q-factor at ambient conditions**

Possible sources of dissipation:

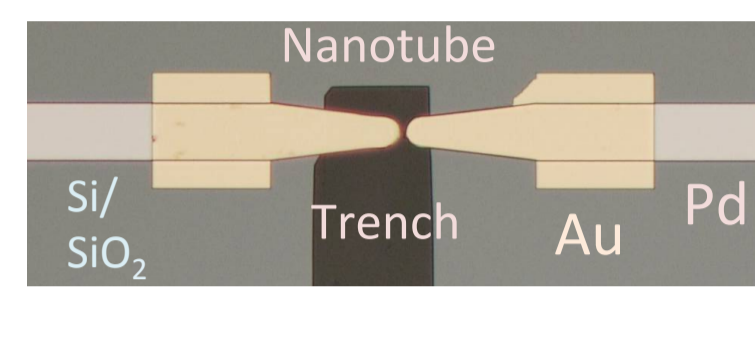
- Gas damping
- Defect scattering
- Intrinsic phonon-phonon dissipation
- Thermoelastic losses
- Clamping/anchor losses**



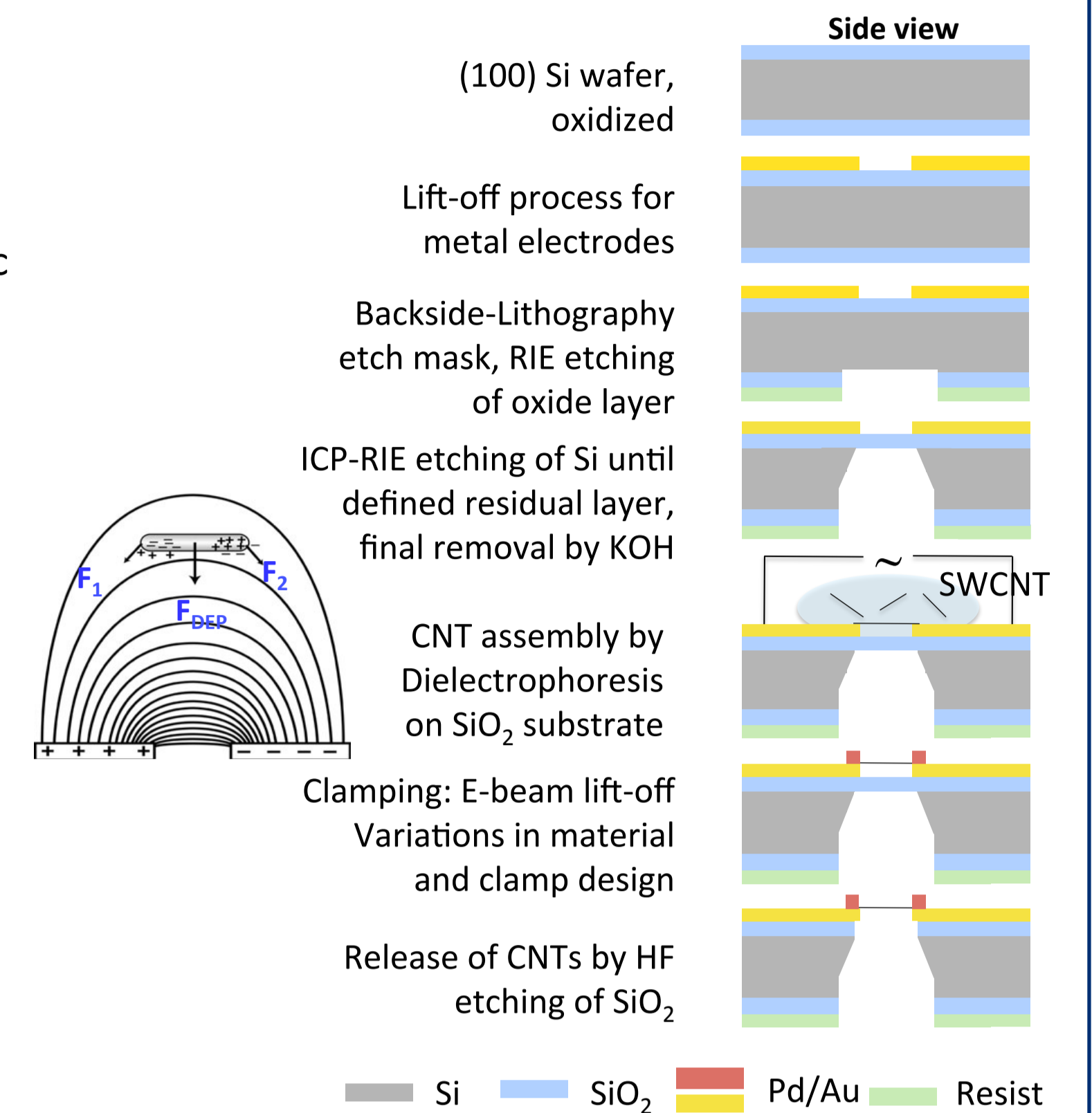
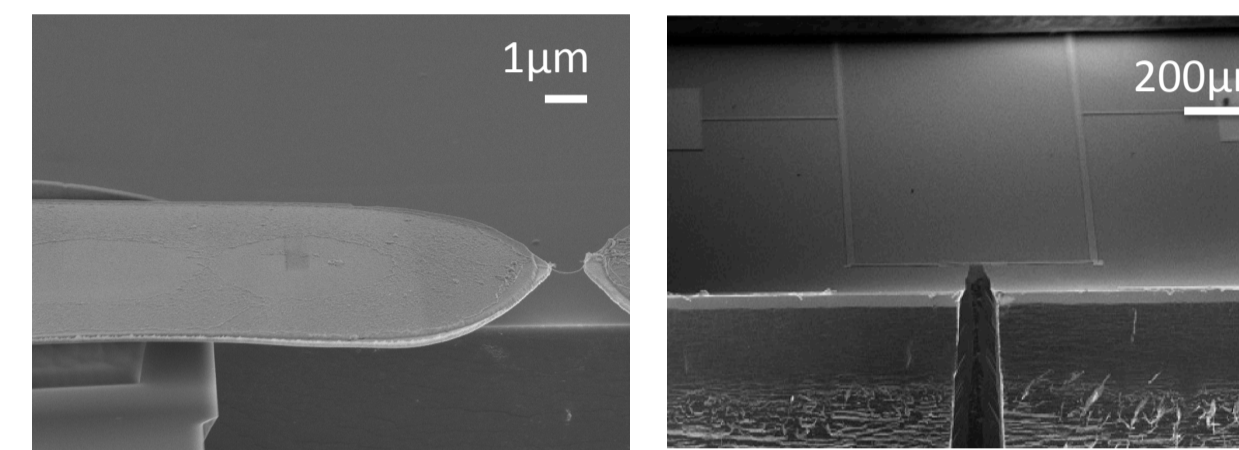
**Target: Develop nanomanipulation techniques for in situ determination of mechanical properties of SWNTs and evaluation of the clamping quality for different contacts**

### Device Fabrication

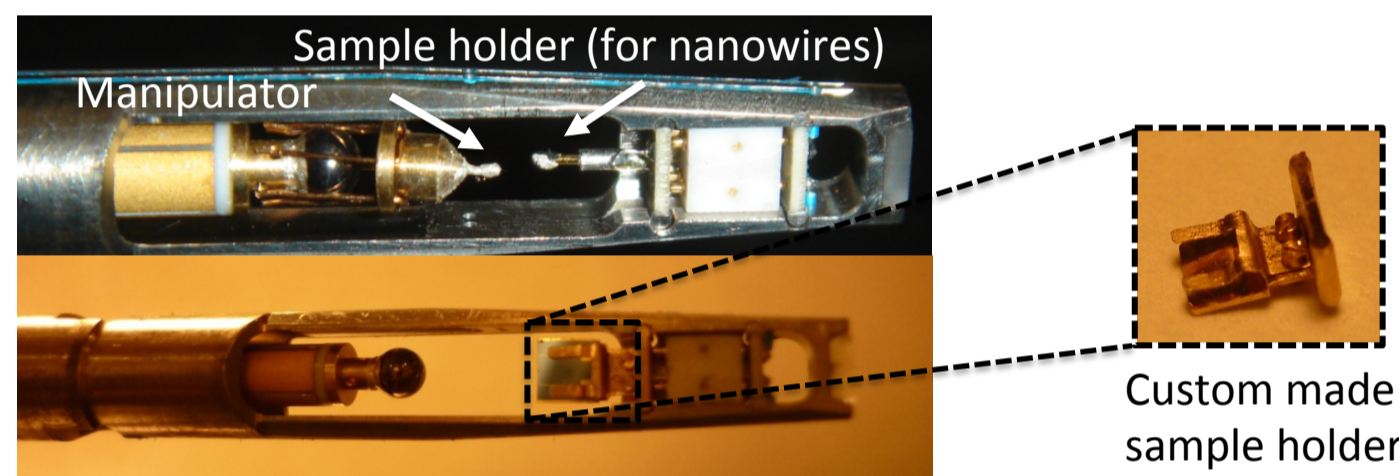
**Task:** Design of devices that are amenable to manipulation in TEM and SEM based microrobotic systems and in AFM [2]



Trenches are needed for accessibility and visibility (projection in TEM)

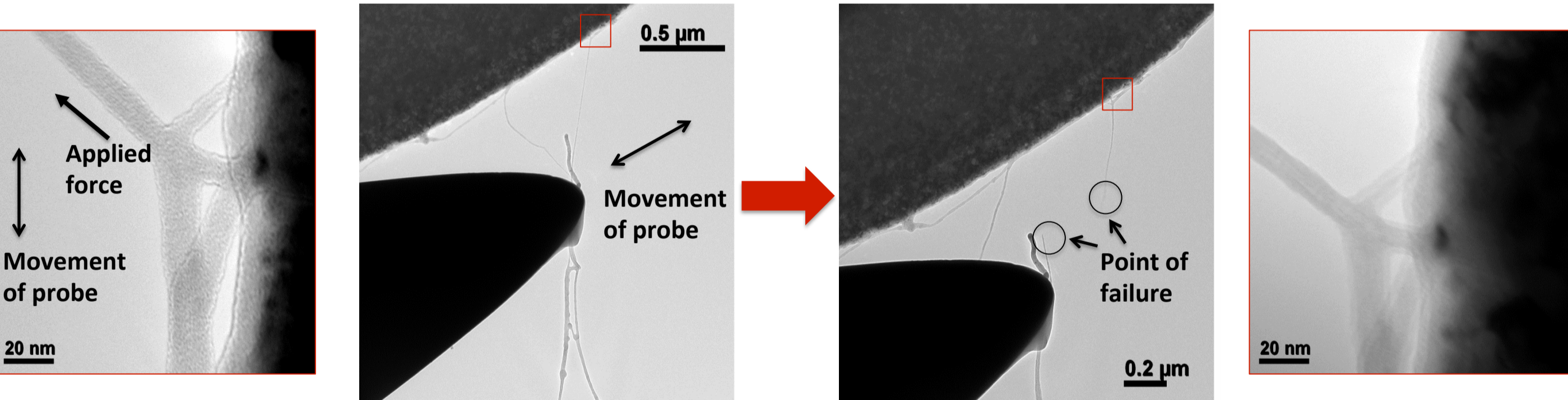


### TEM manipulation



Commercial manipulation set-up (Nanofactory) for manipulation of nanowires. A special holder was designed for in-situ device testing

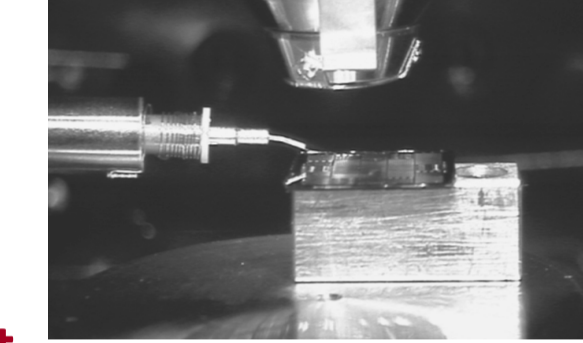
**Manipulation sequence:** probe-CNT contact by EBID, applied tensile strength by retraction of probe



Inside TEM: device in manipulation holder, approaching tungsten probe through trench on the left side. The CNT and probe are aligned in z by moving the probe into focus

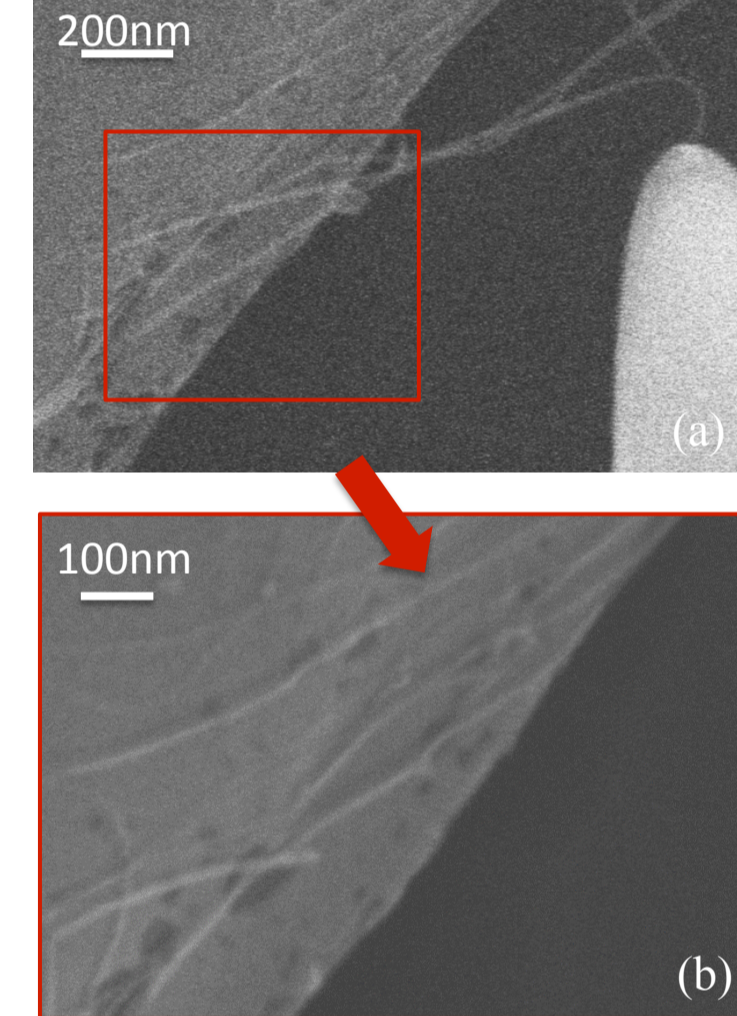
### SEM manipulation

Manipulation set-up in SEM 2/3 of the chip is mounted on a solid block with carbon tape. The trench is freely accessible.



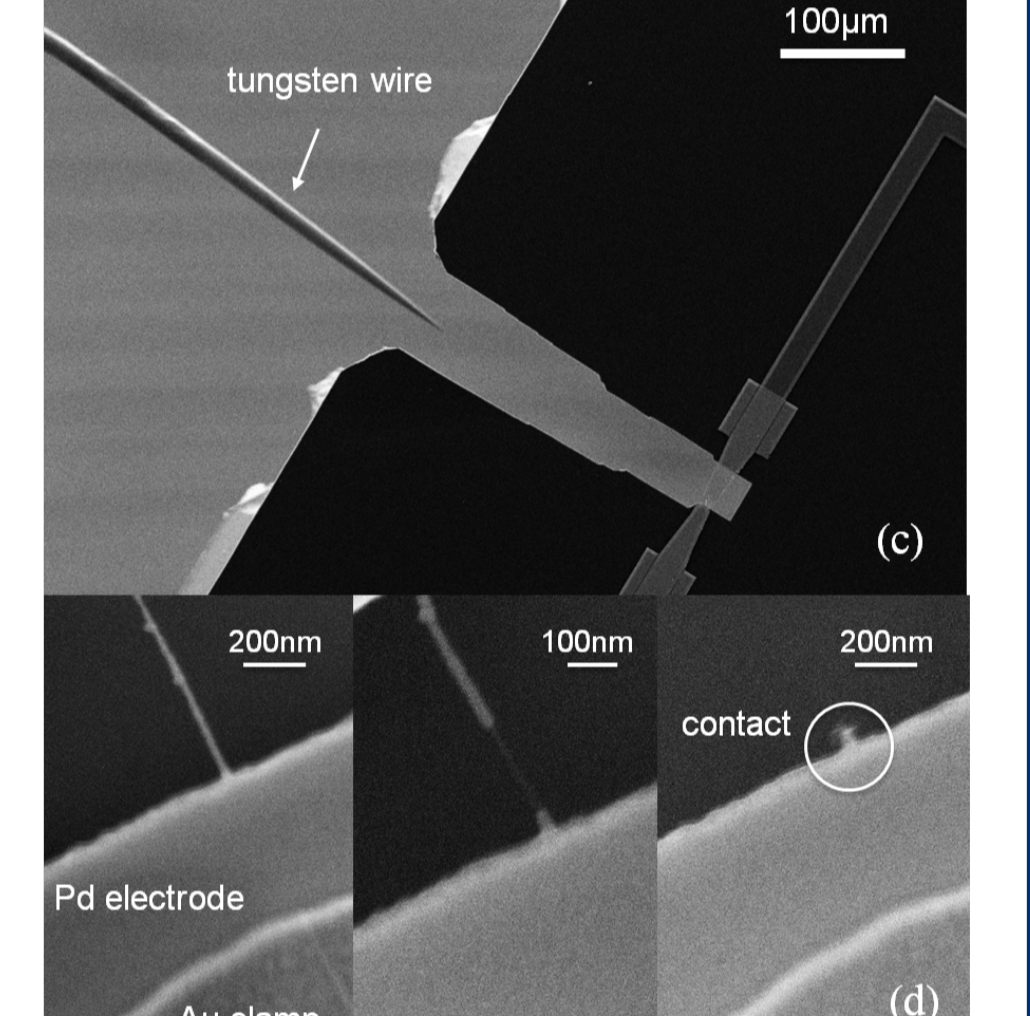
SEM micromanipulator (Kleindiek Nanotechnik) The probe consists of a sharp tungsten wire attached to a 1mm thick copper shaft.

**Without clamping: Failure at contact**

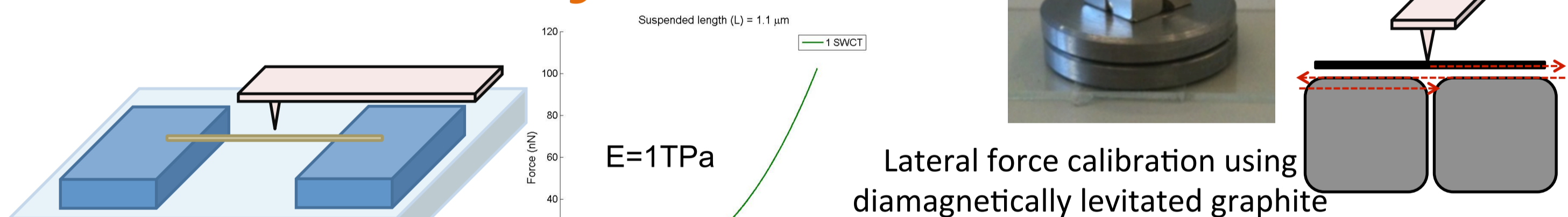


**Right: With top EBL clamp**  
For about 10 SWNTs tested the failure occurs outside the clamping contacts  
**Strong clamping achieved**

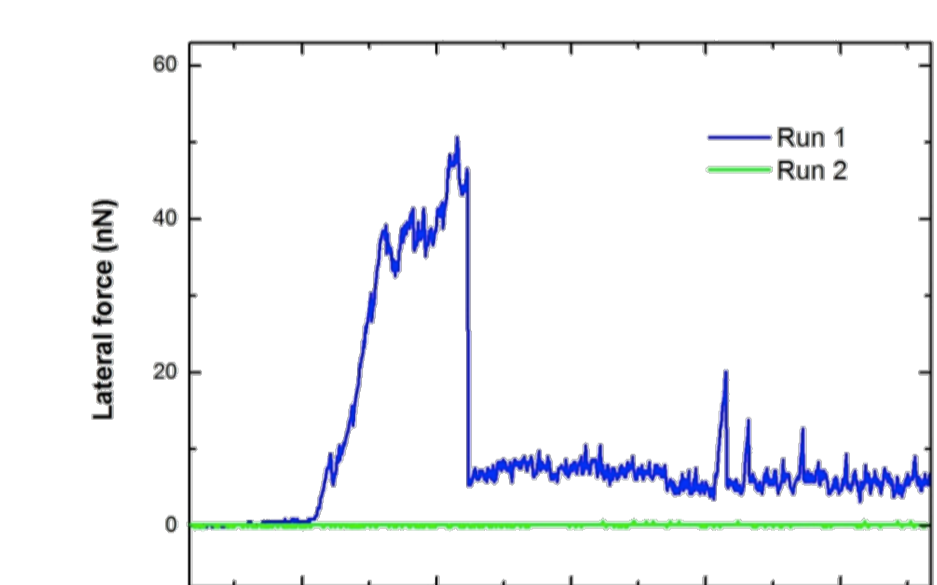
**With clamping: Failure at the CNT**



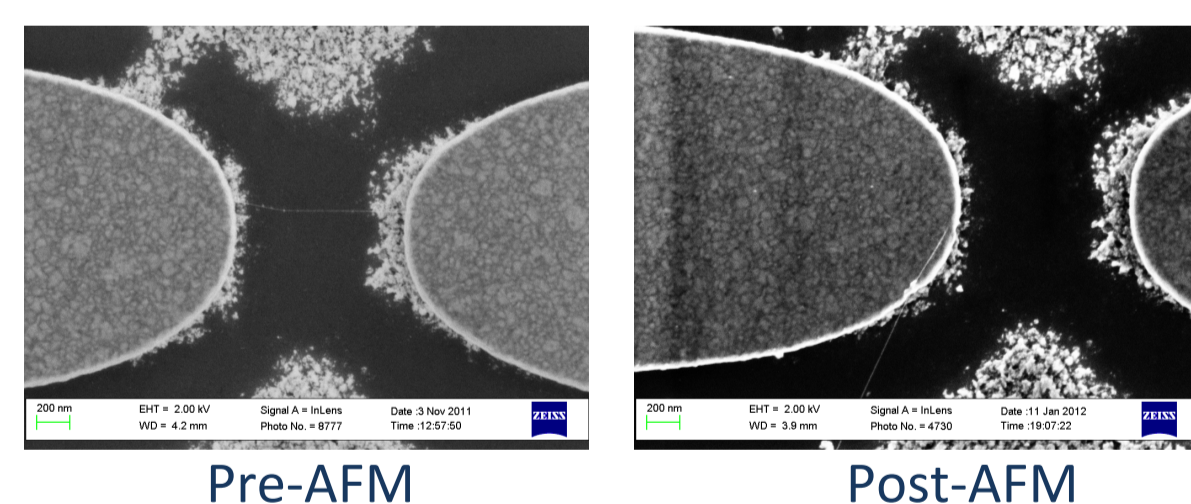
### Lateral AFM deflection



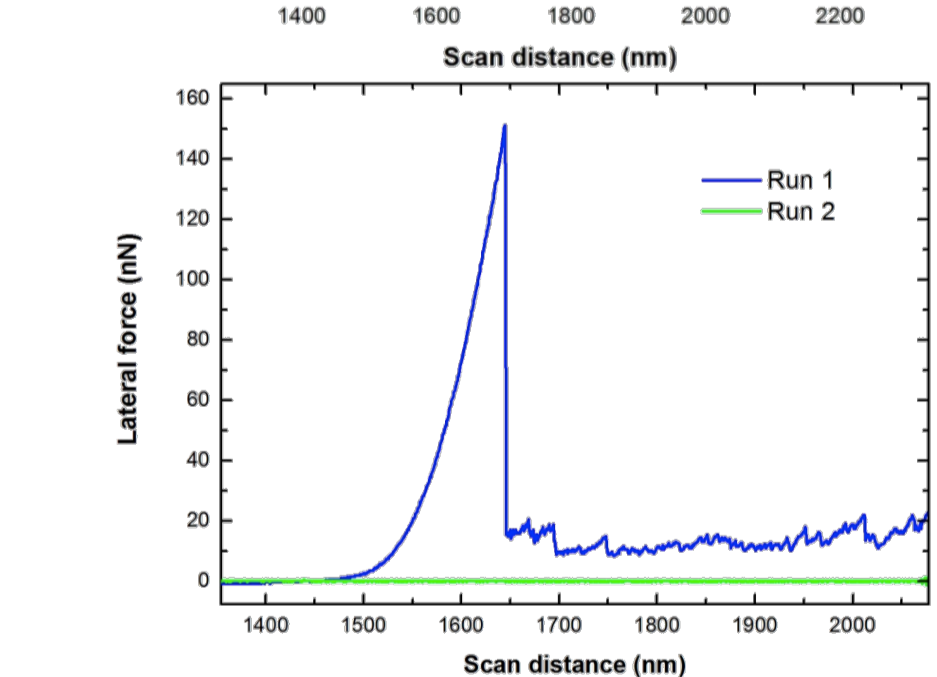
Lateral deflection of suspended nanowire/nanotube with AFM tip using nanomanipulation strategy in MFP-3D AFM



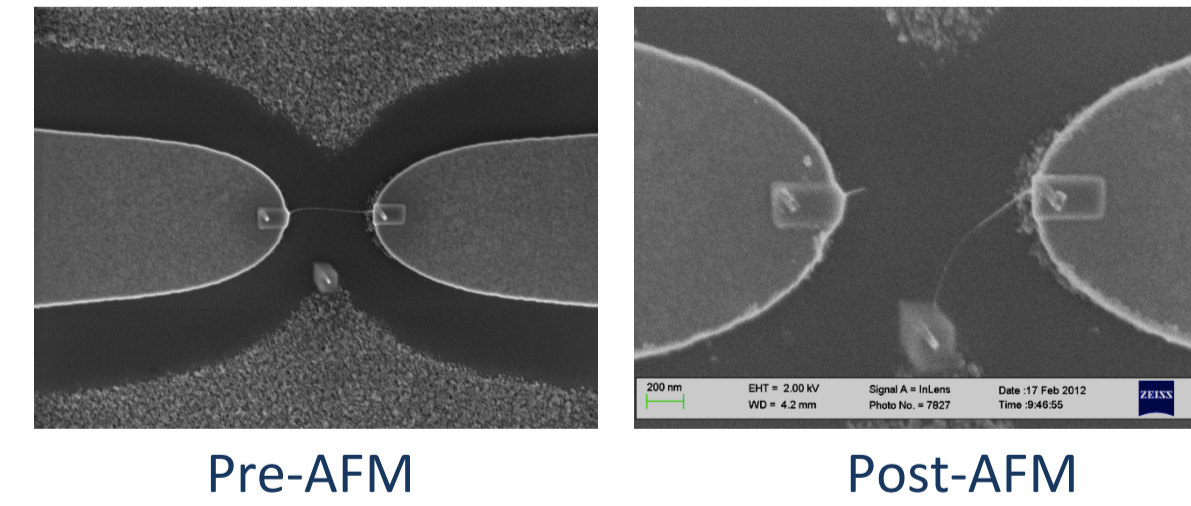
**Au electrode without clamp**



Nearly ~85 nm deflection is sustained before slippage  
About 1.4% stretching of the SWCNT before failure (suspended length: ~1µm)

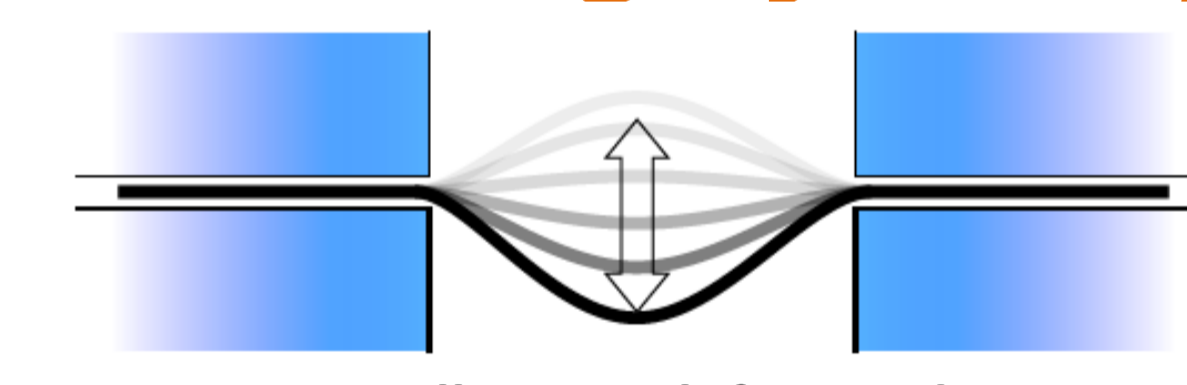


**Au electrode with Pt-clamp**

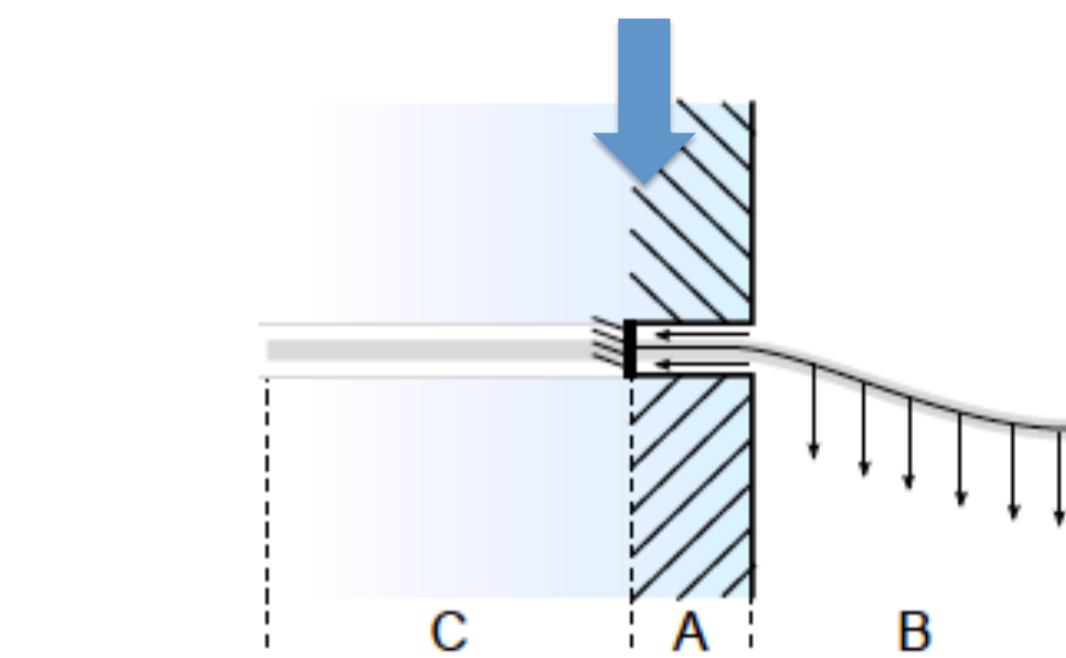


Nearly ~150 nm deflection is sustained before failure  
About 4.4% stretching of the SWCNT before failure (suspended length: ~1µm)

### Modeling of Damping by Slippage



Oscillator with free ends



Simplified model of CNT oscillator with fixed ends

Decoupling into 2 problems:

A: longitudinal response  $v(x,t) = \sum_{m=1}^{\infty} h_m(t) \sin(n\frac{\pi}{2l}x)$

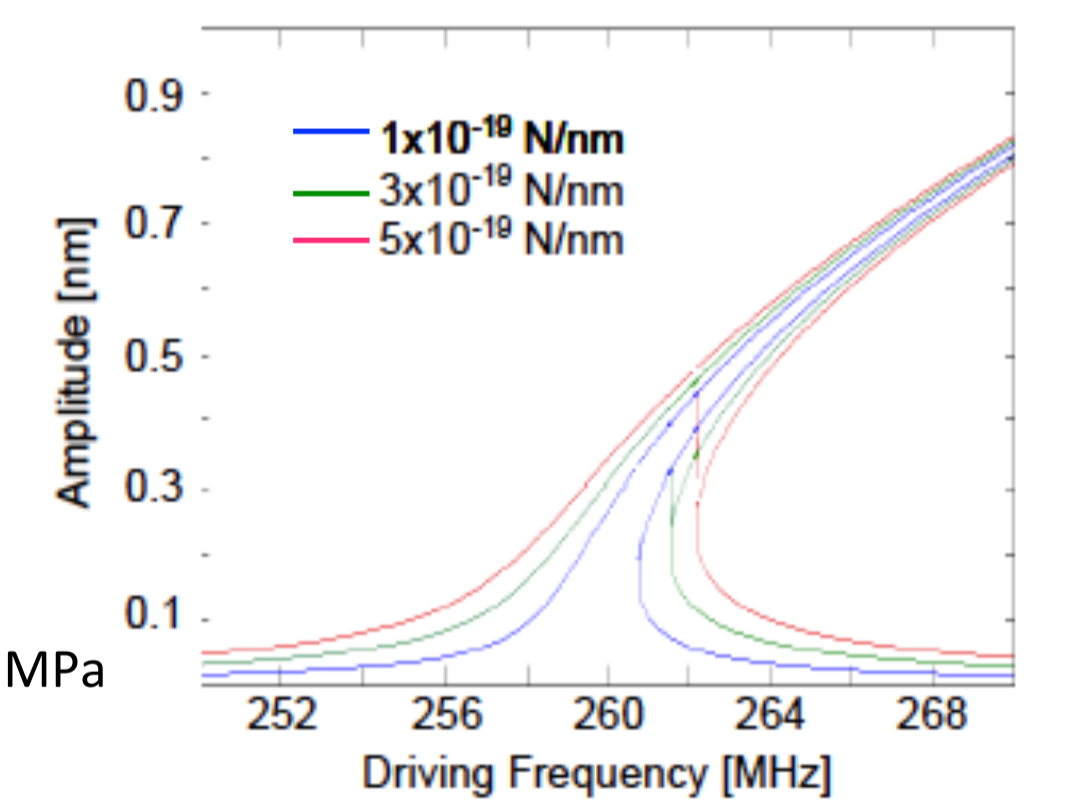
$$h_m\left(\frac{t_p}{4}\right) = 0 \quad \text{for } m = 1, 3, 5, \dots$$

$$\dot{h}_m\left(\frac{t_p}{4}\right) = 0 \quad h_m(t) = \frac{4}{m\pi d} \sqrt{\frac{Ipd}{E}} (-1)^{\frac{m-1}{2}} \int_{\frac{t_p}{4}}^{t_p} s(t') \sin\left[\frac{m\pi}{2} \sqrt{\frac{E}{Ipd}} (t-t')\right] dt'$$

B: transverse response

$$u(x,t) = \left[ A \cos(\omega t) + \beta_1 \frac{A^3}{32\alpha_1} [\cos(3\omega t) - \cos(\omega t)] \right] \sin\left(\frac{\pi}{L}x\right)$$

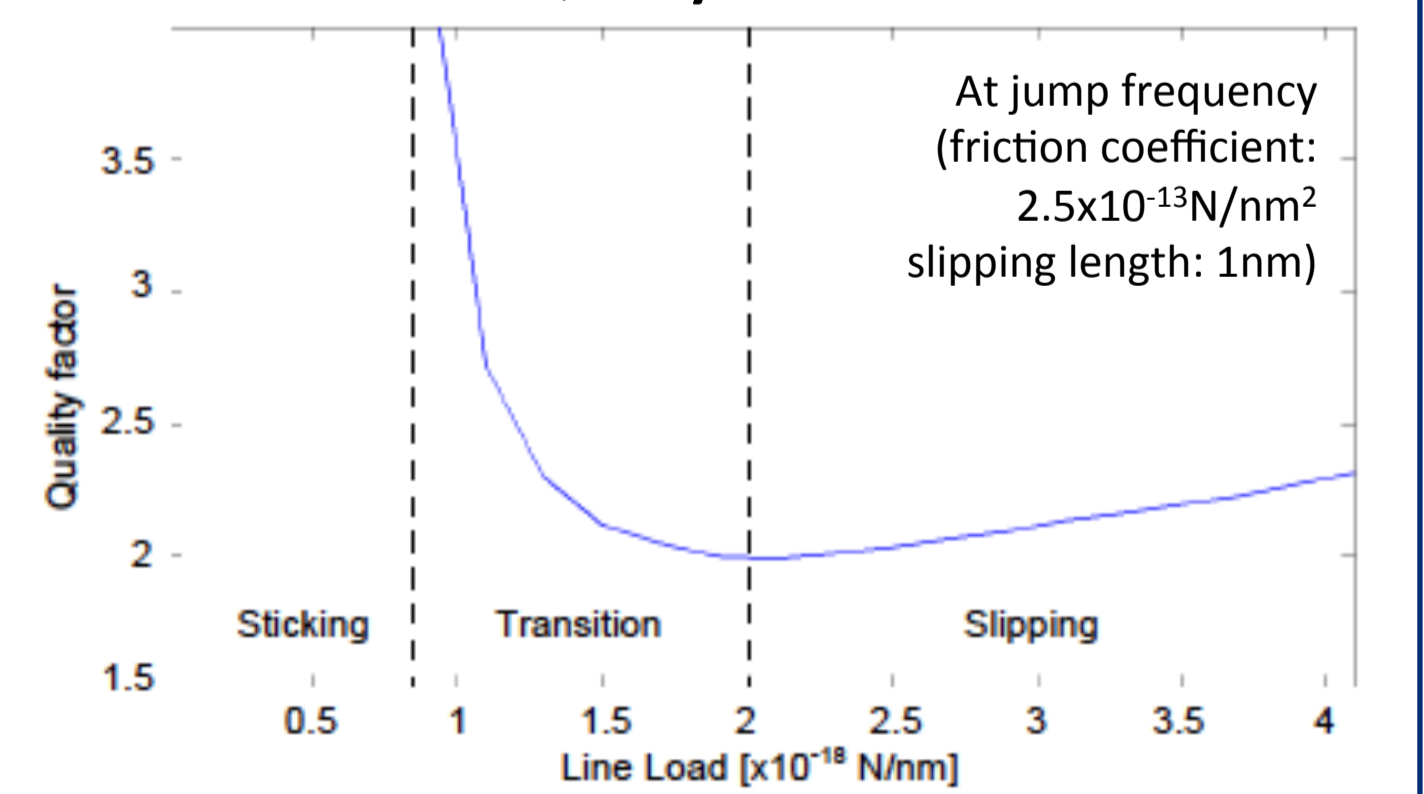
Non-linear damped oscillator



l = 1µm, d = 1nm  
initial tension: 15MPa

Analytical results in good agreement with theory  
Hardening nonlinearity  
Increase of jump frequency with larger driving force

Quality factor



### Conclusions

- Experimental Results:**  
Additional clamping reduces slipping as shown qualitatively and quantitatively by SEM, TEM and AFM manipulation methods, and hence should help achieve high Q-factors
- Analytical model:**
  - Slipping friction equivalent to linear damping
  - Transition from sticking to slipping friction leads to decreasing quality factors with increasing forces, as most prominent characteristic of nonlinear damping

### References

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