

Estimating the Real-Time Respiratory Rate from the ECG with a Bank of Notch Filters

Leila Mirmohamadsadeghi, Jean-Marc Vesin



Applied Signal Processing Group, Swiss Federal Institute of Technology EPFL, Lausanne, Switzerland



Introduction

- Goal:** Estimate the respiratory rate from the heart beat (ECG) with low delay
- Waveforms:**
 - Respiratory sinus arrhythmia (RSA)
 - Respiratory modulation of R-peak amplitudes (RPA)
- State-of-the-art:** Fast Fourier transform or adaptive filters
- Shortcomings:** Large delays
- Proposed algorithm:** based on the outputs of a bank of notch filters

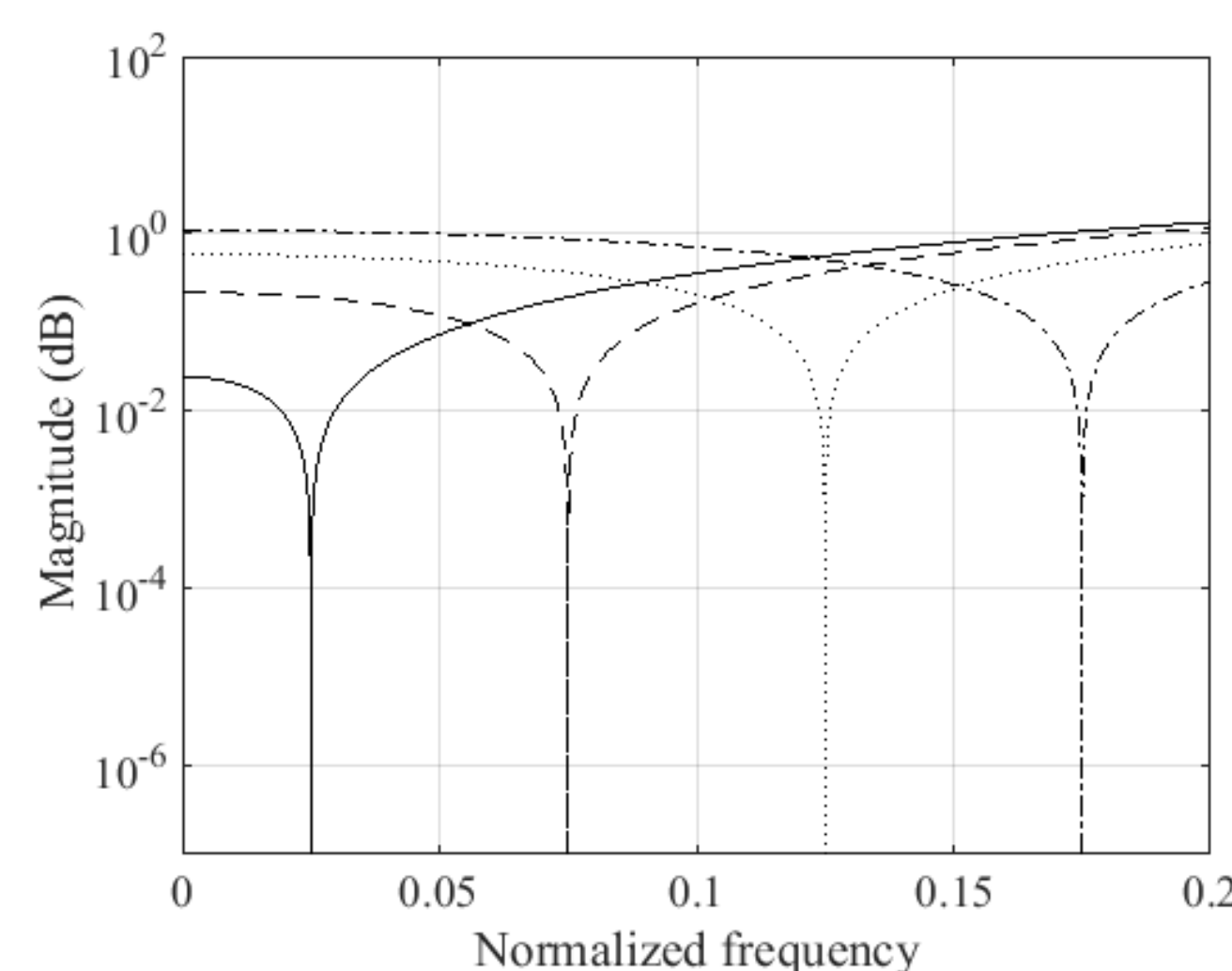
Conclusions

- Respiratory rate estimates are **accurate** (lower error than the state-of-the-art)
- The estimates have **low delays**
- Algorithm is **moderately sensitive** to its parameters
- ✓ **Good candidate for mobile health monitoring, e.g., with a smart-shirt as in ObeSense**

Methods

Algorithm input

- RSA: heart beat-to-beat distances
- RPA: heart beat amplitudes
 - re-sampled @ 4 Hz
 - filtered 0.1-0.5 Hz



Algorithm flow

Order-3 FIR filters

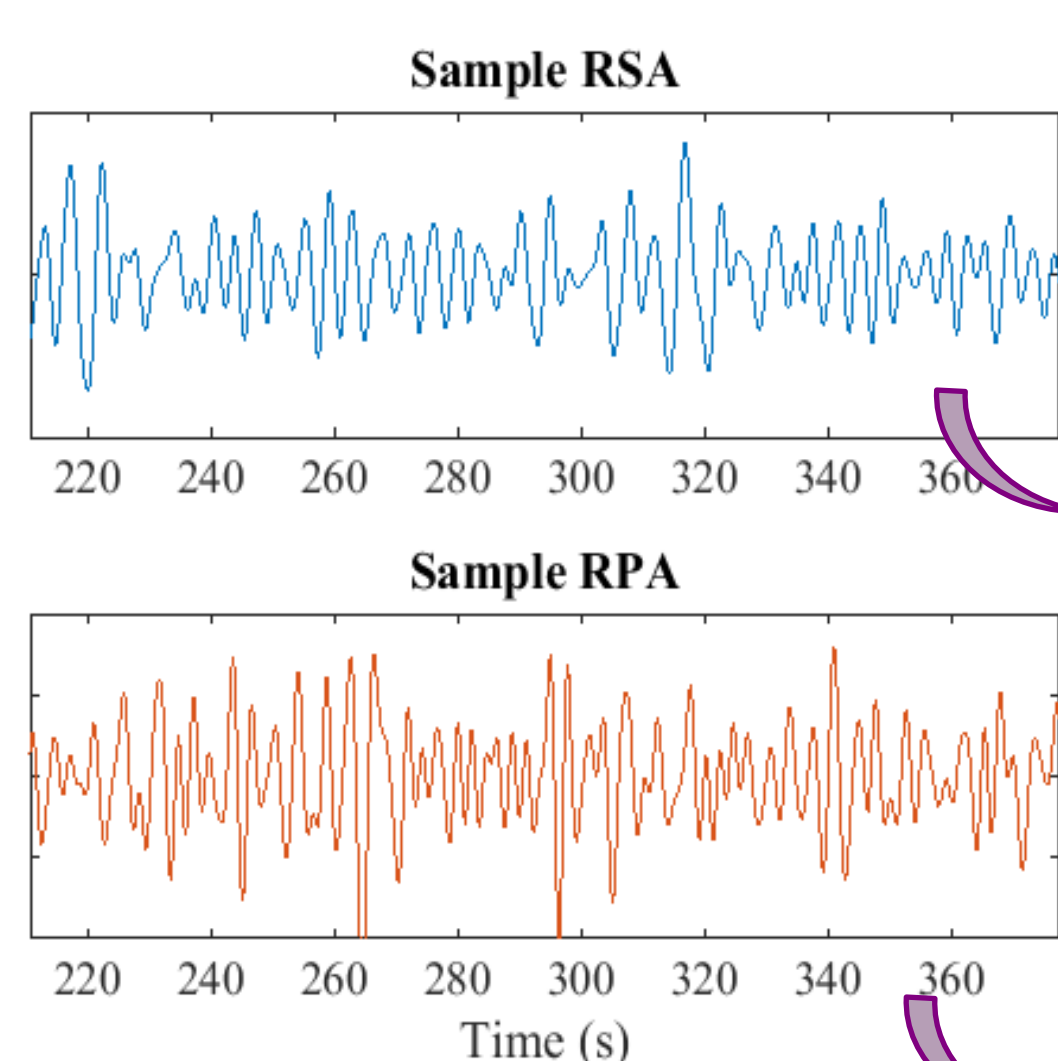
$$\text{Eq. 1: } H(z) = 1 - 2z^{-1} \cos(2\pi f_i) + z^{-2}$$

$$\text{Eq. 2: } y_i[n] = u[n] - 2u[n-1] \cos(2\pi f_i) + u[n-2]$$

$$\text{Eq. 6: } w_i[n] = \frac{1}{N_{sig}} \sum_{j=1}^{N_{sig}} P_{i,j}[n]$$

$$\text{Eq. 7: } W_i[n] = \exp\left(-\min_i P_{i,j}[n] w_i[n]\right)$$

Averaging: single weight over all inputs
Exp: large weights for small powers



$$\text{Eq. 5: } U[n] = \delta U[n-1] + (1-\delta)u^2[n]$$

Recursive mean square value

$$\text{Eq. 3: } P_i[n] = \delta P_i[n-1] + (1-\delta)c_i^2[n]$$

$$\text{Eq. 4: } c_i[n] = y_i[n]/\sqrt{U[n]}$$

Recursive output normalized with respect to input

$$\text{Eq. 8: } f[n] = \frac{\sum_{i=1}^N W_i[n] f_i}{\sum_{i=1}^N W_i[n]}$$

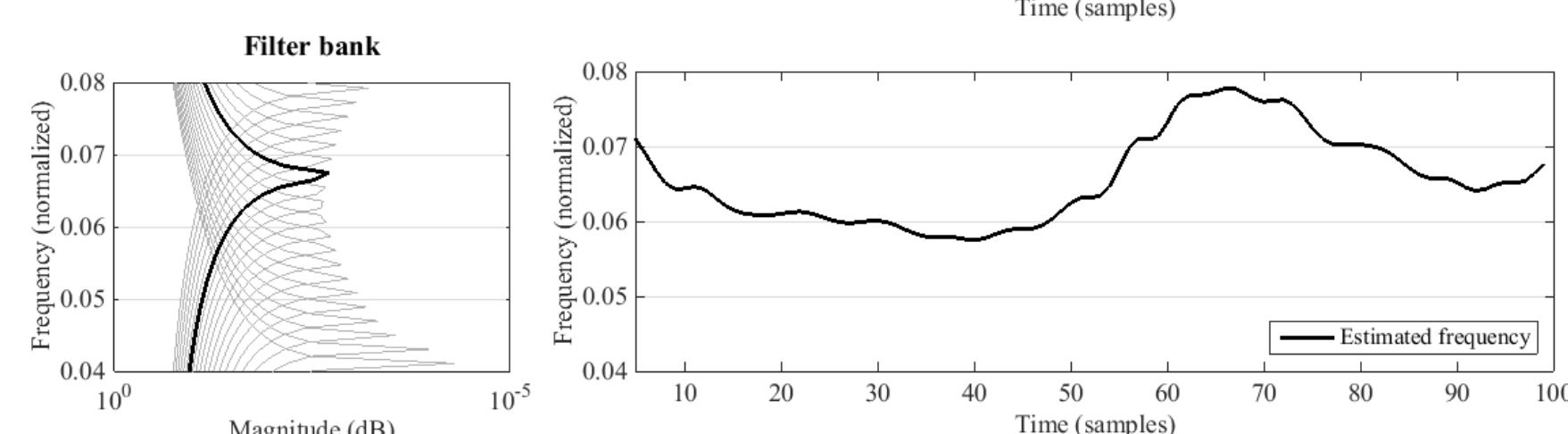
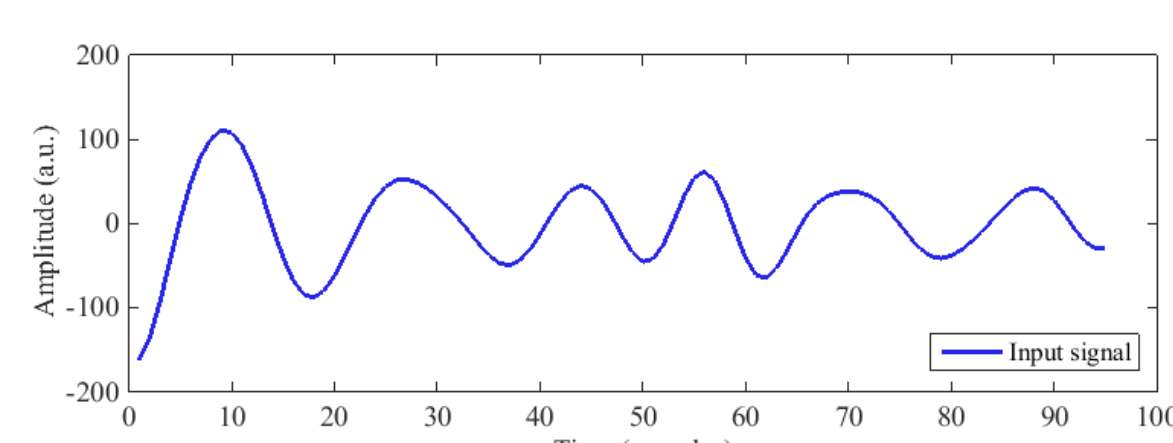
Algorithm output:
f: frequency estimate.
Weighted sum of notch frequencies

Results

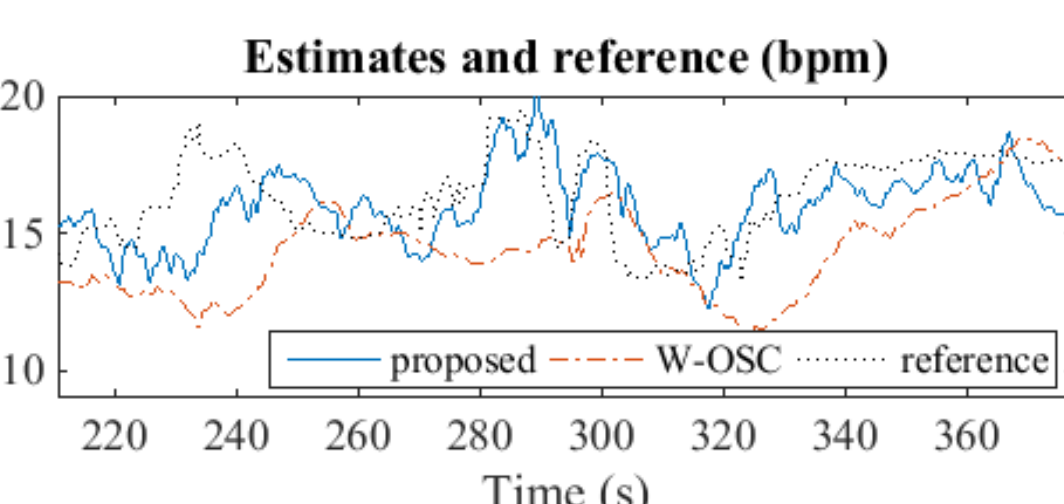
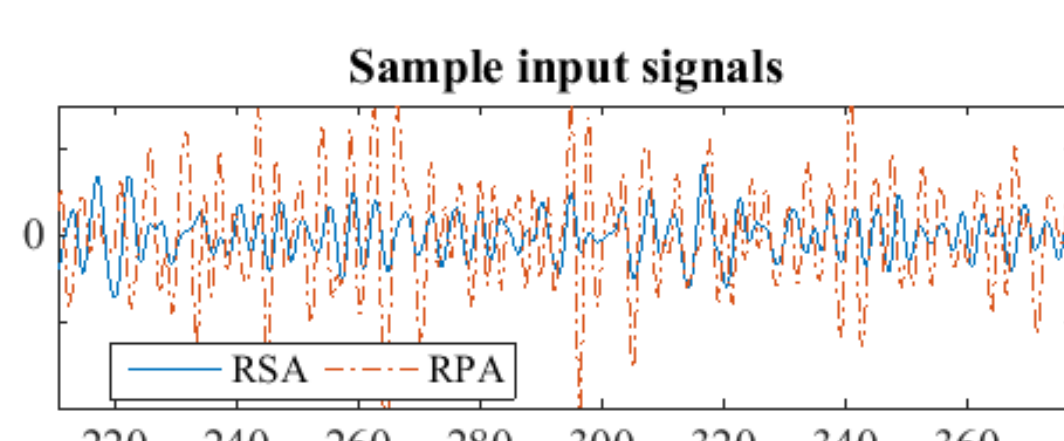
Illustration of the algorithm

- With a single input:

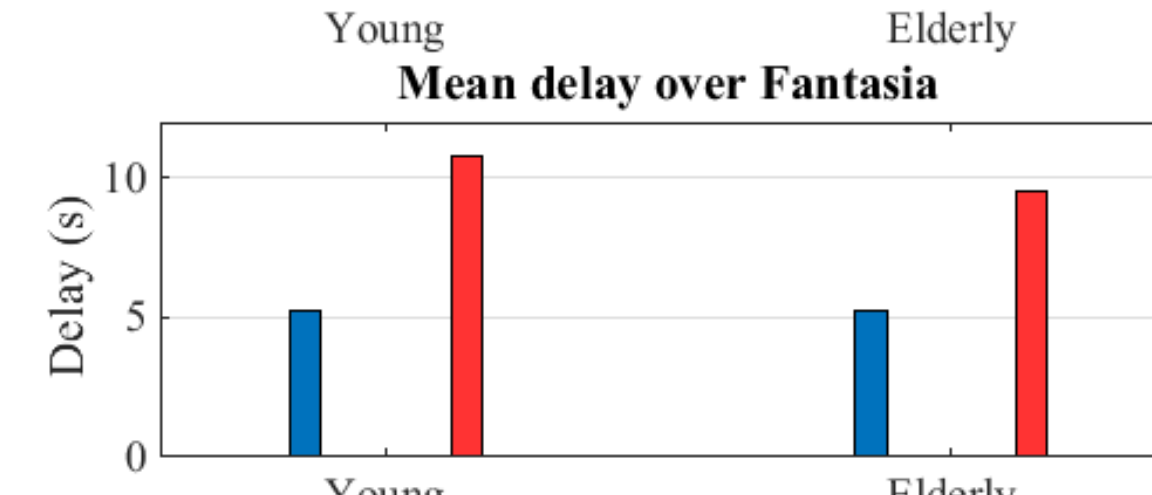
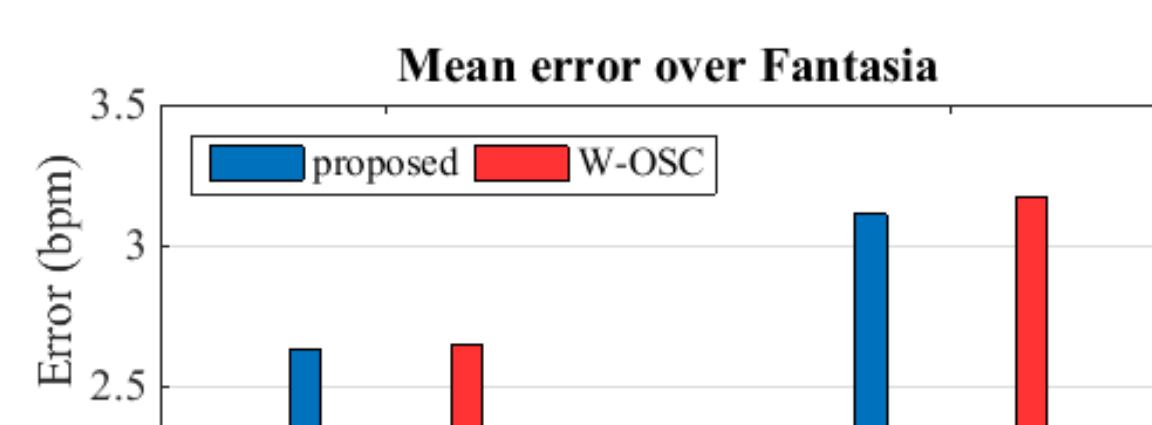
Link to video:



- With two inputs:



Performance



✓ Lower error than the W-OSC

✓ Half the delay of the W-OSC

✓ Moderate (low) sensitivity

- Mean absolute error (bpm)
- Delay (seconds, measured by correlation analysis)
- Comparison to the state-of-the-art adaptive filter (W_ OSC method [1])

[1] Mirmohamadsadeghi and Vesin, Biomed Signal Process Control, 2014

- High N: less quantization ↔ more computations
- High δ: less variability ↔ slower adaptation

Sensitivity analysis

